

Unit	Lesson	Lesson Objectives
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**Extending the Number System****Operations on Rational and Irrational Numbers**

Explain why the product of a nonzero rational number and an irrational number is irrational.

Explain why the sum and product of two rational numbers are rational.

Explain why the sum of a rational number and an irrational number is irrational.

**Complex Numbers**

Determine the absolute value of a complex number.

Represent complex numbers in the form  $a + bi$  or in the complex plane.

Represent square roots of negative numbers as multiples of  $i$ .

Simplify powers of  $i$  using their cyclic nature.

**Operations with Complex Numbers**

Identify the field properties of complex numbers.

Perform addition, subtraction, and multiplication of complex numbers.

**Function Operations**

Combine functions using arithmetic operations, expressing the results both algebraically and graphically.

Evaluate sums, differences, products, and quotients of functions.

**Function Inverses**

Find the inverse of a function.

Use composition to verify that functions are inverses.

**Solving Equations**

Create multistep equations in one variable and use them to solve problems.

Simplify and solve multistep equations

**Recognizing Patterns**

Analyze a sequence of numbers to determine the pattern, and identify whether it is arithmetic or geometric.

Use a recursive rule to calculate a term of a sequence.

Write a recursive rule for a sequence.

**Radicals****Laws of Exponents**

Apply the properties of whole-number exponents to generate equivalent expressions.

**Simplifying Nonperfect Roots**

Simplify nonperfect roots without rationalizing.

**Rational Exponents**

Evaluate numeric expressions using properties of rational exponents.

Simplify algebraic expressions using properties of rational exponents.

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		<p><b>Adding and Subtracting Radicals</b></p> <p>Add and subtract radical expressions.</p> <p>Identify like radicals.</p> <p><b>Multiplying Radicals</b></p> <p>Perform multiplication of radical expressions.</p> <p><b>Dividing Radicals</b></p> <p>Perform division of radical expressions, rationalizing the denominator when necessary.</p>
		<p><b>Quadratic Functions</b></p> <p><b>Introduction to Quadratic Functions</b></p> <p>Calculate the rate of change of a quadratic function over an interval of its domain, and compare it to linear and exponential functions.</p> <p>Evaluate a quadratic function using tables, graphs, and equations.</p> <p>Identify a quadratic function and the values of the coefficients and constant from the standard form.</p> <p><b>Quadratic Functions: Standard Form</b></p> <p>Graph a quadratic function given in standard form, identifying the key features of the graph.</p> <p><b>Completing the Square</b></p> <p>Determine key aspects of the graph of a quadratic function given in standard form and with <math>a = 1</math> by writing it in vertex form.</p> <p>Relate the geometric model of completing the square to the algebraic process.</p> <p>Relate the parameters of a quadratic function in vertex form to transformations of the graph <math>y = x^2</math>.</p> <p>Write quadratic functions given in standard form and with <math>a = 1</math> into vertex form by completing the square.</p> <p><b>Completing the Square (Continued)</b></p> <p>Determine key aspects of the graph of a quadratic function given in standard form by writing it in vertex form.</p> <p>Relate the parameters of a quadratic function in vertex form to transformations of the graph <math>y = x^2</math>.</p> <p>Write quadratic functions given in standard form into vertex form by completing the square.</p> <p><b>Comparing Exponential, Linear, and Quadratic Growth</b></p> <p>Use tables and graphs to compare the growth of an exponential function to the growth of a linear function over equal intervals.</p> <p>Use tables and graphs to compare the growth of an exponential function to the growth of a quadratic or a polynomial function over equal intervals.</p> <p>Use tables and graphs to show that exponential functions grow by equal factors over equal intervals.</p> <p><b>Quadratic Inequalities</b></p> <p>Create quadratic inequalities in one variable and use them to solve problems.</p> <p>Find real solutions of quadratic inequalities algebraically and graphically.</p>

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**Solving Quadratic Equations****Solving Quadratic Equations: Zero Product Property**

Solve problems by factoring quadratic equations given in standard form.

Write quadratic equations given rational solutions.

**Solving Quadratic Equations by Factoring**

Find real solutions for quadratic equations using the zero product property.

Use key attributes of a quadratic function to solve word problems.

**Solving Quadratic Equations: Square Root Property**

Use the square root property to solve quadratic equations.

**Solving Quadratic Equations: Completing the Square**

Solve a quadratic equation whose leading coefficient is 1 by completing the square.

**Completing the Square**

Find complex solutions to quadratic equations by completing the square.

Recognize the pattern of a perfect-square trinomial as the square of a binomial.

Use the square root property to solve equations.

**Introduction to the Quadratic Formula**

Determine the values of  $a$ ,  $b$ , and  $c$  from a given quadratic equation in standard form.

Justify the steps used to derive the quadratic formula by completing the square.

Recognize an expression that uses the quadratic formula to find the solutions of a quadratic equation.

Relate the discriminant in the quadratic formula to the types of solutions of a quadratic equation.

**The Quadratic Formula**

Find real and complex solutions of quadratic equations using the quadratic formula.

Use the discriminant to determine the number and type of roots of a quadratic equation.

**Modeling with Quadratic Equations**

Write and solve quadratic equations to model real-world scenarios, estimating where appropriate and identifying solutions that are not viable in terms of the context.

**Solving Linear-Quadratic Systems**

Solve a system of equations consisting of a line and a parabola algebraically and graphically, using technology where appropriate.

**Regression Models**

Determine an exponential, quadratic, or linear model for a given data set using technology.

Identify limitations of models in real-world contexts.

Interpret the graph of a regression model in the context of the problem.

Use a linear, quadratic, or exponential regression model to make a prediction.

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**Polynomial Expressions****Introduction to Polynomials**

Classify a polynomial by degree and number of terms.

Identify a polynomial and its equivalent forms.

**Adding and Subtracting Polynomials**

Add and subtract polynomials, determining the degree and number of terms of the sum or difference.

Find and evaluate polynomial sums or differences that model real-world situations.

**Multiplying Monomials and Binomials**

Identify a product that results in the difference of squares or a perfect square trinomial.

Multiply a binomial by a monomial or binomial algebraically and by using geometric models.

**Multiplying Polynomials and Simplifying Expressions**

Interpret the structure of an expression involving addition, subtraction, and multiplication of polynomials in order to write it as a single polynomial in standard form.

Multiply a binomial by a trinomial algebraically and by using geometric models.

**Factoring Polynomials: GCF**

Determine an appropriate way to factor a polynomial for a given context.

Determine the greatest common monomial factor of two or more terms.

Write a polynomial as the product of a monomial and polynomial having the same number of terms.

**Factoring Polynomials: Double Grouping**

Factor a polynomial by double grouping or indicate that the polynomial is prime.

**Factoring Trinomials:  $a = 1$** 

Determine if a trinomial with a leading coefficient of 1 and a positive constant is factorable and, if so, write it in factored form.

Relate the factorization of a trinomial with a leading coefficient of 1 and a positive constant to a geometric model.

**Factoring Trinomials:  $a = 1$  (Continued)**

Determine if a trinomial with a leading coefficient of 1 and a negative constant is factorable and, if so, write it in factored form.

Relate the factorization of a trinomial with a leading coefficient of 1 and a negative constant to a geometric model.

**Factoring Trinomials:  $a > 1$** 

Determine if a trinomial with a leading coefficient greater than 1 is factorable and, if so, write it in factored form.

Relate the factorization of a trinomial with a leading coefficient greater than 1 to a geometric model.

**Factoring Polynomials: Difference of Squares**

Determine if a polynomial is factorable by recognizing that it is a difference of two squares and, if so, applying the identity.

Identify a monomial that is a perfect square and find the square root.

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**Angle and Triangle Relationships****Special Angle Pairs**

- Calculate angle measures by using definitions and theorems about special angle pairs
- Define and identify special angle pairs

**Congruent Angle Pairs**

- Apply theorems about congruent angle pairs to calculate angle measures
- Identify angle relationships by using theorems about congruent angle pairs

**Parallel Lines and Angles**

- Apply theorems about angles formed by parallel lines cut by a transversal to calculate angle measures
- Identify angle pairs formed by lines cut by a transversal

**Interactive: Proving Angles Congruent**

- Prove angle relationships given parallel lines cut by a transversal

**Proving Lines Parallel**

- Calculate angle measures in order to justify that lines are parallel
- Identify theorems used to justify that lines are parallel
- Prove lines are parallel using various proof formats

**Bisectors in a Triangle**

- Apply properties of bisectors of a triangle to solve problems
- Identify the properties of the circumcenter and incenter of a triangle

**Medians and Altitudes of a Triangle**

- Apply properties of medians and altitudes of a triangle to solve problems
- Identify the properties of the orthocenter and centroid of a triangle

**Midsegments of a Triangle**

- Apply the triangle midsegment theorem to solve problems
- Identify the triangle midsegment theorem and use it to justify relationships

**Isosceles Triangles**

- Apply theorems related to isosceles triangles to solve problems
- Identify theorems related to isosceles triangles and use them to justify side and angle relationships

**Pythagorean Theorem**

- Apply the Pythagorean theorem to find side lengths of a right triangle
- Solve problems using the Pythagorean theorem in modeling situations

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**Proportional Geometry****Dilations****Similar Polygons**

- Identify and apply properties of similar polygons
- Use proportions to solve problems involving similar polygons

**Similar Triangles**

- Calculate angle measures and side lengths of similar triangles
- Identify and apply the AA similarity postulate and the SSS and SAS similarity theorems

**Right Triangle Similarity**

- Apply theorems to solve problems involving geometric means
- Identify similar right triangles formed by an altitude and write a similarity statement

**Interactive: Proving Triangles Similar**

- Complete proofs involving similar triangles

**Special Segments and Proportions**

- Solve problems using theorems about special segments and triangles

**Perimeter and Area of Similar Figures**

- Identify the relationships between the side lengths, perimeters, and areas of similar figures
- Use the relationships between similar figures to calculate perimeters and areas

**Introduction to Trigonometry and Quadrilaterals****Right Triangles**

- Determine the sine, cosine, and tangent of an acute angle by using technology
- Determine the sine, cosine, and tangent of an angle using right triangles
- Identify sides and corresponding angles of a right triangle
- Use proportions to determine side lengths of similar right triangles

**Special Right Triangles**

- Solve problems involving special right triangles in modeling situations
- Use properties of  $45^\circ$ - $45^\circ$ - $90^\circ$  and  $30^\circ$ - $60^\circ$ - $90^\circ$  triangles to find side lengths

**Trigonometric Ratios**

- Apply trigonometric relationships to complementary angles to write equivalent expressions
- Determine the exact values of sine, cosine, and tangent for  $30^\circ$ ,  $45^\circ$ , and  $60^\circ$
- Identify and apply the trigonometric ratios of sine, cosine, and tangent

**Solving Right Triangles**

- Solve problems involving right triangles in modeling situations
- Use trigonometric ratios to find missing parts of a right triangle

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**Angles of Elevation and Depression**

- Identify angles of elevation and depression in problem situations
- Solve problems involving angles of elevation and depression

**Evaluating the Six Trigonometric Functions**

- Evaluate the six trigonometric functions for angles in degrees or radians based on one or more given trigonometric function values.
- Evaluate the six trigonometric functions for angles in degrees or radians given a point on the terminal ray.

**Classifying Quadrilaterals**

- Apply properties of various quadrilaterals to calculate angle measures and side lengths
- Apply the quadrilateral angle sum theorem to calculate angle measures
- Classify and describe relationships within the family of quadrilaterals

**Properties of Parallelograms**

- Apply theorems about parallelograms to calculate angle and segment measures
- Complete proofs involving properties of parallelograms
- Identify theorems about the properties of parallelograms

**Proving a Quadrilateral Is a Parallelogram**

- Identify and apply theorems that determine if a quadrilateral is a parallelogram
- Prove a quadrilateral is a parallelogram

**Special Parallelograms**

- Apply theorems about special parallelograms to calculate angle and segment measures
- Complete proofs involving the diagonals of special parallelograms
- Identify theorems about the diagonals of rectangles, rhombi, and squares

**Interactive: Proving Special Parallelograms**

- Complete proofs involving rectangles, rhombi, and squares

**Circles****Introduction to Circles**

- Calculate the circumference and area of a circle
- Identify terms related to circles
- Solve problems related to circles in modeling situations

**Tangents to a Circle**

- Complete proofs involving the relationships between tangents and circles
- Identify and apply theorems about tangents and radii
- Identify common tangents between circles

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### **Arcs, Chords, and Central Angles**

- Complete proofs involving the relationships between arcs and chords of a circle
- Identify relationships between arcs and central angles and apply them to solve problems
- Identify theorems about arcs and chords and apply them to solve problems

### **Inscribed Angles**

- Calculate the measures of angles and their intercepted arcs
- Complete proofs involving the relationships of angles and arcs of a circle
- Identify relationships between inscribed angles and arcs

### **Secants, Tangents, and Angles**

- Identify relationships between arcs and angles formed by secants, tangents, and chords
- Solve problems involving angles and arcs formed by secants, tangents, and chords

### **Special Segments**

- Calculate the lengths of segments formed by chords, secants, and tangents
- Identify relationships between segments formed by chords, secants, and tangents

### **Arc Length and Area of a Sector**

- Calculate arc lengths
- Calculate the areas of sectors and segments of circles
- Relate the degree and radian measures of an angle

### **Interactive: Circle Constructions**

- Use a straightedge and compass to create constructions involving circles

### **Construct Regular Polygons**

- Construct regular polygons inscribed in a circle.
- Prove that all circles are similar.

## **Dimensions and Algebraic Connections**

### **Volume**

- Calculate the volume of prisms, cylinders, pyramids, and cones
- Describe the effect on volume when the dimensions of a solid figure are changed
- Solve problems involving the volume of prisms, cylinders, pyramids, and cones

### **Spheres**

- Apply the formulas for volume and surface area of a sphere to determine unknown measurements.
- Use given measurements of a sphere or hemisphere to find the volume or surface area.



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**Similar Solids**

- Calculate the surface areas and volumes of similar solids
- Identify the relationships between the surface areas and volumes of similar solids

**Geometric Figures in the Coordinate Plane**

- Complete proofs involving geometric figures in the coordinate plane
- Use coordinate geometry to verify the properties of a geometric figure

**Conic Sections: Circles**

- Given specific information about a circle, determine its equation in standard form
- Given the equation of a circle in standard form, identify the center, the radius, and the graph

**Conic Sections: Parabolas**

- Relate the algebraic and geometric representations of parabolas

**Applications of Probability****Set Theory**

- Find subsets, complements, and cross products of sets
- Identify and describe the relationships and the notation used in set theory

**Venn Diagrams and Sets**

- Use symbolic notation to describe events displayed in Venn diagrams involving unions, intersections, and complements
- Use Venn diagrams to explore set relationships
- Use Venn diagrams to solve problems involving sets

**Random Behavior**

- Apply lists, diagrams, and the fundamental counting principle to determine the number of outcomes possible in a given situation
- Identify experimental and theoretical probabilities and apply the law of large numbers to determine probabilities

**Mutually Exclusive and Independent Events**

- Calculate probabilities using the addition rule of mutually exclusive events
- Calculate probabilities using the multiplication rule of independent events
- Identify and describe mutually exclusive and independent events

**Conditional Probability**

- Use calculations to determine if two events are independent
- Use formulas and Venn diagrams to calculate conditional probabilities
- Use general probability rules to calculate probabilities of compound events

**Geometric Probability**

- Calculate geometric probability using segment and area models
- Solve problems involving geometric probability in modeling situations

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		<b>Probability and Two-Way Tables</b> <ul style="list-style-type: none"><li>Calculate conditional probabilities from data displayed in a two-way table</li><li>Use a two-way table to determine if two events are independent</li></ul>
		<b>Decision Making Using Probability</b> <ul style="list-style-type: none"><li>Calculate probabilities and make decisions in modeling situations</li><li>Construct a theoretical probability model from all possible outcomes</li></ul>
		<b>Probability with Combinations and Permutations</b> <ul style="list-style-type: none"><li>Quantify outcomes using combinations and permutations</li><li>Use combinations and permutations to compute probabilities of compound events</li></ul>
		<b>Nonlinear Functions and Transformations</b>
		<b>Absolute Value Functions</b> <ul style="list-style-type: none"><li>Analyze absolute value functions to determine key features of the graph.</li><li>Model and solve mathematical and real-world problems with absolute value functions.</li></ul>
		<b>Step Functions</b> <ul style="list-style-type: none"><li>Analyze step functions to determine key features of the graph.</li><li>Evaluate step functions.</li><li>Use step functions to model real-world problems.</li></ul>
		<b>Piecewise Defined Functions</b> <ul style="list-style-type: none"><li>Determine the domain, range, and continuity of piecewise defined functions.</li><li>Evaluate piecewise defined functions.</li><li>Graph piecewise defined functions.</li></ul>
		<b>Transformations of Quadratic Functions</b> <ul style="list-style-type: none"><li>Describe the effects of changes in <math>a</math>, <math>h</math>, and <math>k</math> to the graph of a function in the form <math>y = a(x - h)^2 + k</math>.</li><li>Use completing the square to write quadratic functions in the form <math>y = a(x - h)^2 + k</math>.</li></ul>
		<b>Transformations of Functions</b> <ul style="list-style-type: none"><li>Analyze a function rule or graph to determine transformations of the parent function.</li><li>Identify a function as belonging to a family of functions.</li></ul>
		<b>Modeling with Functions</b> <ul style="list-style-type: none"><li>Find the equation of a function that best models a data set.</li><li>Use function models to solve problems.</li></ul>