

Unit	Lesson	Lesson Objectives
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**Functions and Modeling****Graphs of Rational Functions**

Analyze key features of a rational function.

Graph a rational function.

Use algebraic techniques to determine key features of a rational function.

**Domain and Range**

Determine the domain and range of a function in both mathematical and real-world contexts.

**Functions and Transformations**

Describe the effect of one or more transformations on the graph of a function.

Graph a transformation of a function.

Recognize even and odd functions.

Write the equation of a transformed function given its graph.

**Composition of Functions and Modeling**

Identify the functions that make up a composite function.

Justify why function composition is not commutative.

Use a composition of two functions to model and solve a real-world problem.

**Comparing a Function and Its Inverse**

Compare and contrast characteristics of a function and its inverse.

Verify two functions are inverses of each other using graphs or tables.

**Inverse of a Function**

Determine the additive or multiplicative inverse of a function or its characteristics.

Determine values of an inverse function from a table or graph.

Find the inverse of a function, restricting the domain when necessary.

Verify that functions are inverses.

**Equations and Inequalities****Polynomial Inequalities**

Apply polynomial inequalities to mathematical and real-world problems.

Solve polynomial inequalities having real coefficients.

**Rational Inequalities**

Solve rational inequalities algebraically and determine extraneous solutions.

**Solving Exponential and Logarithmic Equations**

Solve exponential and logarithmic equations using inverses, properties, and algorithms.

**Modeling with Exponential and Logarithmic Equations**

Model and solve real-world problems using exponential and logarithmic functions.

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**Exponential and Logarithmic Inequalities**

- Interpret a graphical solution to an exponential or logarithmic inequality.
- Solve a problem by graphing an exponential or logarithmic inequality.

**Exponential, Logistic and Logarithmic Models**

- Interpret the numeric values in an exponential, logarithmic, or logistic function in terms of a context.
- Model a problem using an exponential, logarithmic, or logistic function.
- Solve a problem using an exponential, logarithmic, or logistic function.

**Regression Analysis**

- Interpret a calculator-generated equation in terms of the data it represents.
- Use a calculator-generated equation to draw conclusions or make predictions.
- Use technology to find an appropriate model (polynomial, exponential, trigonometric, power, logistic, or logarithmic) for a given data set.

**Performance Task: Logistic Models****Trigonometry****Angles and Trigonometric Functions**

- Convert between radian and degree measure.
- Evaluate trigonometric functions.
- Use the unit circle to explain key features of the sine and cosine functions.
- Use trigonometric functions to solve problems.

**Linear and Angular Velocity**

- Solve problems involving angular velocity.
- Solve problems involving linear velocity.

**Graphing Sine and Cosine Functions**

- Describe the result of a stretch, compression, or reflection over the  $x$ -axis on the sine or cosine function.
- Graph a stretch, compression, or reflection over the  $x$ -axis of the sine or cosine function.
- Graph the sine or cosine function, attending to units on the horizontal axis.
- Interpret key features of a sine or cosine function that models a real-world context.

**General Form of Sine and Cosine**

- Create an appropriate periodic function to model a real-world context.
- Describe the result of a vertical or horizontal shift on the sine or cosine function.
- Graph a vertical or horizontal shift of the sine or cosine function.
- Interpret key features of a sine or cosine function that models a real-world context.

**Graphing Cosecant and Secant Functions**

- Analyze key features of secant and cosecant functions from equations and graphs.

**Graphing Tangent and Cotangent**

- Analyze key features of tangent and cotangent functions from equations and graphs.

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**Inverse Trigonometric Functions**

- Determine the key features of an inverse trigonometric function.
- Evaluate expressions containing inverse trigonometric functions.
- Graph an inverse trigonometric function.
- Use inverse functions to solve trigonometric equations that model real-world scenarios.

**Performance Task: Modeling with Sinusoidal Functions****Analytic Trigonometry****Trigonometric Difference Identities**

- Prove the trigonometric subtraction identities for sine, cosine, or tangent.
- Solve a trigonometric equation involving a subtraction identity for sine, cosine, or tangent.
- Use a trigonometric subtraction identity for sine, cosine, or tangent to find the exact trigonometric value of an angle.
- Use a trigonometric subtraction identity for sine, cosine, or tangent to simplify an expression or verify an identity.

**Trigonometric Sum Identities**

- Prove the trigonometric addition identity for sine, cosine, or tangent.
- Solve a trigonometric equation involving an addition identity for sine, cosine, or tangent.
- Use a trigonometric addition identity for sine, cosine, or tangent to find the exact trigonometric value of an angle.
- Use a trigonometric addition identity for sine, cosine, or tangent to simplify an expression or verify an identity.

**Trigonometric Double Angle Identities**

- Prove the trigonometric double angle identities for sine, cosine, or tangent.
- Solve a trigonometric equation involving a double angle identity for sine, cosine, or tangent.
- Use a trigonometric double angle identity for sine, cosine, or tangent to find the exact trigonometric value of an angle.
- Use a trigonometric double angle identity for sine, cosine, or tangent to simplify an expression or verify an identity.

**Trigonometric Half Angle Identities**

- Prove the trigonometric half-angle identity for sine, cosine, or tangent.
- Solve a trigonometric equation involving a half-angle identity for sine, cosine, or tangent.
- Use a trigonometric half-angle identity for sine, cosine, or tangent to find the exact trigonometric value of an angle.
- Use a trigonometric half-angle identity for sine, cosine, or tangent to simplify an expression or verify an identity.

**Solving Trigonometric Equations**

- Analyze key features of inverse trigonometric functions from equations and graphs.
- Evaluate inverse trigonometric functions over a specified domain.
- Solve trigonometric equations over a specified domain.

**Solving Trigonometric Inequalities**

- Solve trigonometric inequalities by graphing.

**Performance Task: Trigonometric Identities**

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**Complex Numbers and Polar Coordinates****Performing Operations with Complex Numbers**

Identify the field properties of complex numbers.

Perform addition, subtraction, multiplication, and division of complex numbers.

**Distance and Midpoints in the Complex Plane**

Calculate the modulus of a complex number.

Solve problems involving distances and midpoints in the complex plane.

Use the average to find the midpoint of a segment in the complex plane.

Use the modulus to find the distance between any two complex numbers in the plane.

**Polar Form of Complex Numbers**

Convert between the rectangular and polar form of a complex number, or between rectangular and polar coordinates.

Explain why the rectangular and polar forms of a given complex number represent the same number.

Find conjugates, moduli, and arguments of complex numbers.

Graph points in the complex or polar plane given polar coordinates or the rectangular or polar form of a complex number.

**Graphing Polar Equations**

Convert between polar and rectangular equations.

Graph or describe the graph of a polar equation.

Solve a problem involving one or more polar equations.

Use a polar equation to represent a real-world scenario or interpret parts of a polar equation in terms of a context.

**Add and Subtract Complex Numbers**

Find a sum or difference of complex numbers.

Identify a geometric representation for the sum or difference of complex numbers.

**Multiply and Divide Complex Numbers**

Find a product or quotient of complex numbers.

Identify a geometric representation for the product or quotient of complex numbers.

**Powers and Roots of Complex Numbers**

Find roots of complex numbers.

Prove de Moivre's theorem.

Use de Moivre's theorem to calculate a power of a complex number.

**Vectors****Vectors and Their Components**

Compute the result of multiplying a vector by a scalar.

Determine the direction, magnitude, or components of a vector.

Use multiplication of a vector by a scalar to model or solve a problem.

Unit	Lesson	Lesson Objectives
		<b>Vector Addition and Subtraction</b> <ul style="list-style-type: none"><li>Add vectors geometrically or algebraically.</li><li>Calculate the result of performing two or more of the following operations on vectors: addition, subtraction, scalar multiplication.</li><li>Subtract vectors geometrically or algebraically.</li></ul>
		<b>Law of Sines</b> <ul style="list-style-type: none"><li>Apply the law of sines to solve mathematical and real-world problems.</li><li>Determine whether a triangle has zero, one, or two solutions using the ambiguous case of the law of sines.</li></ul>
		<b>Law of Cosines</b> <ul style="list-style-type: none"><li>Apply the law of cosines to solve mathematical and real-world problems.</li></ul>
		<b>Law of Sines and Law of Cosines — a Deeper Look</b> <ul style="list-style-type: none"><li>Use right triangle trigonometry to develop and prove the Law of Cosines.</li><li>Use right triangle trigonometry to develop and prove the Law of Sines.</li><li>Use the Law of Cosines to solve problems.</li><li>Use the Law of Sines to solve problems.</li></ul>
		<b>Applying Vectors in the Plane</b> <ul style="list-style-type: none"><li>Solve a real-world problem involving vector quantities.</li><li>Use vectors to model a real-world problem.</li><li>Write a trigonometric equation that models a real-world problem involving vectors.</li></ul>
		<b>Dot Product and Work</b> <ul style="list-style-type: none"><li>Calculate the dot product of two vectors.</li><li>Interpret the dot product of two vectors.</li><li>Use the dot product to calculate the angle between two vectors.</li><li>Use the dot product to solve work problems.</li></ul>
		<b>Performance Task: Vector Operations</b>
		<b>Matrices</b>
		<b>Introduction to Matrices</b> <ul style="list-style-type: none"><li>Determine if two matrices are equal.</li><li>Identify types of matrices.</li><li>Represent and interpret data in matrices.</li></ul>
		<b>Adding and Subtracting Matrices</b> <ul style="list-style-type: none"><li>Apply matrix addition to model problems and solve matrix equations.</li><li>Identify and apply the properties of matrix addition.</li><li>Perform matrix addition and subtraction.</li></ul>
		<b>Scalar and Matrix Multiplication</b> <ul style="list-style-type: none"><li>Perform multiplication of a scalar and a matrix.</li><li>Perform multiplication of two matrices.</li></ul>

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		<b>Determinants</b> <ul style="list-style-type: none"><li>Apply determinants to solve problems.</li><li>Evaluate determinants of <math>2 \times 2</math> and <math>3 \times 3</math> matrices.</li></ul>
		<b>Matrices and Their Inverses</b> <ul style="list-style-type: none"><li>Find the inverse of a matrix.</li></ul>
		<b>Solving Matrix Equations</b> <ul style="list-style-type: none"><li>Solve matrix equations by taking the inverse of a matrix.</li><li>Solve matrix equations using operations with matrices.</li></ul>
		<b>Performance Task: Cryptography Using Matrices</b>
		<b>Systems and Matrices</b>
		<b>Cramer's Rule</b> <ul style="list-style-type: none"><li>Solve a system of equations using Cramer's rule.</li></ul>
		<b>Matrices and Row Operations</b> <ul style="list-style-type: none"><li>Perform row operations in matrices.</li><li>Solve a linear system using reduced row echelon form.</li></ul>
		<b>Modeling with Matrices</b> <ul style="list-style-type: none"><li>Model and solve real-world problems using matrices.</li></ul>
		<b>Vector Multiplication Using Matrices</b> <ul style="list-style-type: none"><li>Multiply a vector (regarded as a matrix with one column) by a matrix of suitable dimensions to produce another vector.</li><li>Solve problems involving transformations of vectors using matrices.</li></ul>
		<b>Partial Fractions</b> <ul style="list-style-type: none"><li>Find the partial fraction decomposition of a rational expression.</li><li>Write a rational expression as a sum of fractions that can be used to find the partial decomposition.</li></ul>
		<b>Conic Equations and Graphs</b>
		<b>Conic Sections</b> <ul style="list-style-type: none"><li>Graph or determine key features (center, radius, vertex, directrix, focus) of a circle or parabola from a given equation.</li><li>Identify the conic formed when a plane intersects a double napped cone.</li><li>Write the equation of a circle or parabola given a graph or verbal description.</li></ul>
		<b>Conic Sections: Parabolas</b> <ul style="list-style-type: none"><li>Solve applied problems involving parabolas.</li><li>Use and determine the standard form of the equation of the parabola.</li></ul>
		<b>Equations of Ellipses</b> <ul style="list-style-type: none"><li>Identify the center, foci, directrix, and vertices of an ellipse from an equation or graph.</li><li>Write the equation of an ellipse from a given graph or information about its center, foci, directrix, or vertices.</li></ul>

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**Equations of Hyperbolas**

Determine the foci, directrices, vertices, and asymptotes of a hyperbola with center at the origin from an equation or graph.

Graph a hyperbola with center at the origin from a given equation.

Write the equation of a hyperbola with center at the origin from a given graph or information about its foci, directrices, or vertices.

**Equations of Hyperbolas (continued)**

Determine the center, foci, directrices, vertices, and asymptotes of a hyperbola from an equation or graph.

Write the equation of a hyperbola from a given graph or information about its center, foci, directrices, or vertices.

**The General Equation of Conic Sections**

Complete the square to write the equation of a conic section in standard form.

Determine the type of conic from the general form of a given equation.

Graph, or describe the graph of, a conic from a given equation in general form.

**Performance Task: Graphing Conic Sections****Analytic Geometry****Applications of Conics**

Interpret the constants or coefficients in the equation of a quadratic relation in terms of a context.

Use a quadratic relation to model a problem.

Use a quadratic relation to solve a problem.

**Conic Inequalities**

Graph, or describe how to graph, the solution set of a conic inequality.

Justify the solution of a conic inequality.

**Systems of Inequalities**

Analyze a system of nonlinear inequalities.

Graph a system of nonlinear inequalities.

Solve a mathematical or real-world problem involving a system of nonlinear inequalities.

**Graphing Parametric Equations**

Convert between parametric equations and rectangular relations.

Describe a planar curve given in parametric form.

Graph parametric equations.

Use parametric equations to model problems.

Use parametric equations to solve problems.

**Performance Task: Parametric Equations**

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**Sequences and Series****Arithmetic Sequences**

- Apply the formula of an arithmetic sequence.
- Determine if a sequence is arithmetic.
- Find the common difference of an arithmetic sequence.
- Find the terms of an arithmetic sequence.

**Geometric Sequences**

- Apply the formula of a geometric sequence.
- Determine if a sequence is geometric.
- Find terms of a geometric sequence.
- Find the common ratio of a geometric sequence.

**Summation Notation**

- Convert between series in summation notation and expanded form.
- Evaluate a summation by expanding it.

**Summation Properties and Rules**

- Use summation properties and rules to evaluate sums.

**Arithmetic Series**

- Solve problems using the formula for the sum for an arithmetic series.

**Finite Geometric Series**

- Solve problems using the formula for the sum of a finite geometric series.

**Infinite Geometric Series**

- Determine if an infinite geometric series converges.
- Evaluate the sum of an infinite geometric series.
- Find a partial sum of an infinite geometric series.

**Recursive Formulas**

- Write a rule for a recursively defined function.
- Write the first  $n$  terms of a recursive function given a formula and a term.

**Modeling with Sequences and Series**

- Determine if a sequence or series is arithmetic or geometric.
- Solve real-world problems involving sequences.
- Solve real-world problems involving series.

**Performance Task: Modeling with Sequences and Series**



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**Introduction to Calculus****The Difference Quotient**

Use the difference quotient to calculate an average rate of change.

Write and simplify a difference quotient for a function.

**Understanding the Concept of a Limit**

Determine if a limit exists at a point and if so, its value.

Estimate limits from graphs and tables.

Find one-sided limits from graphs and tables.

**Limits and Continuity**

Apply the extreme value theorem.

Describe the behavior of a function around discontinuities.

Determine the types of discontinuity of a function.

Use limits to determine if a function is continuous at a point.

**Finding Limits**

Find a limit algebraically.

**Limits, Asymptotes, and End Behavior**

Use limits to determine a horizontal asymptote of a function.

Use limits to determine a vertical asymptote of a function.

Use limits to determine the end behavior of a function.

**Limits as They Relate to Sequences and Series**

Determine the error caused when a series is truncated.

Identify a limit of partial sums that represents an infinite series.

Use limits to determine whether a sequence or series converges or diverges.

**Performance Task: Finding and Applying Limits of Functions**